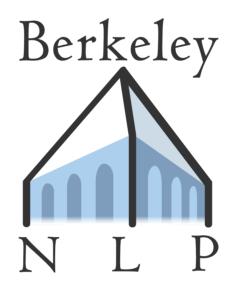
# A Game-Theoretic Approach to Generating Spatial Descriptions

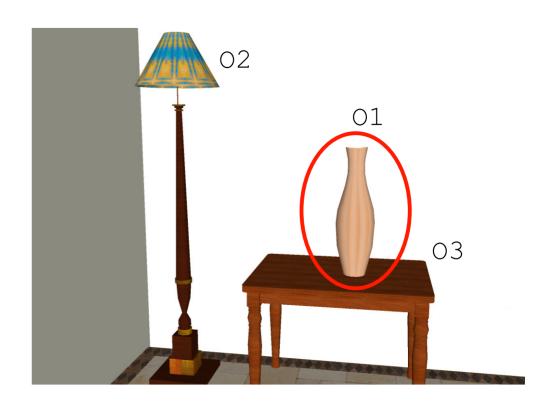
Dave Golland

Percy Liang

Dan Klein

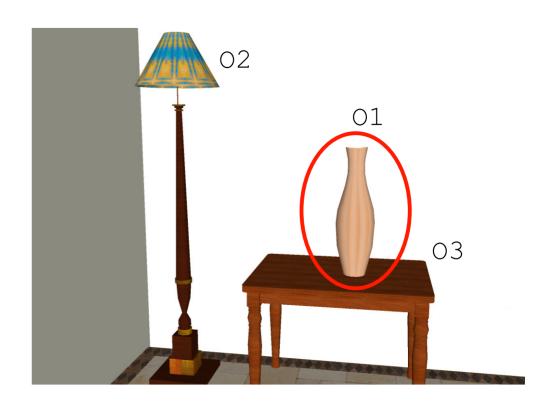


Goal: refer to 01



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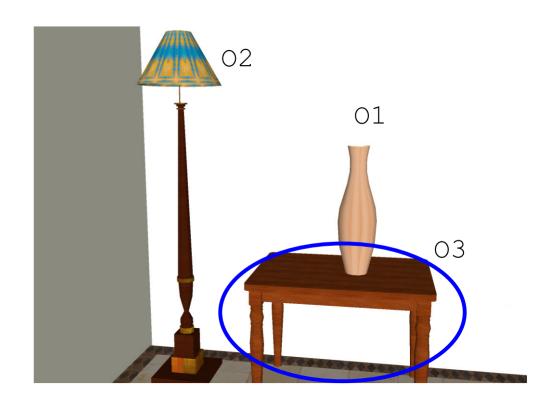
Strategy 1: speak the truth (Maxim of Quality)



Goal: refer to 01

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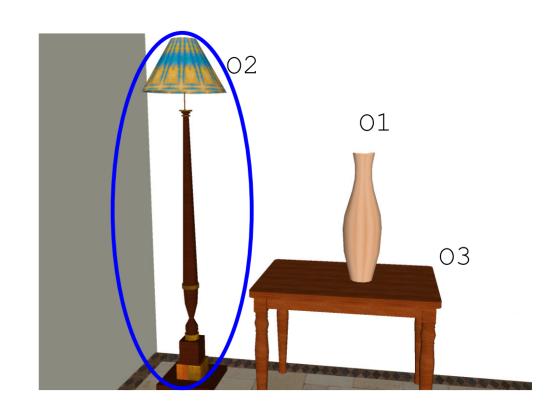
on 03



Goal: refer to 01

Strategy 1: speak the truth (Maxim of Quality)

on 03 right of 02

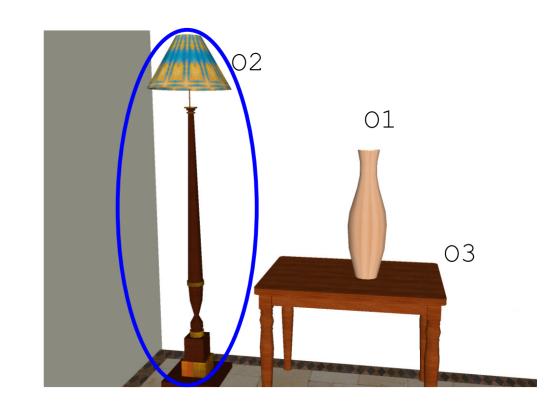


Goal: refer to 01

Strategy 1: speak the truth (Maxim of Quality)

on 03 right of 02

Problem: ambiguity



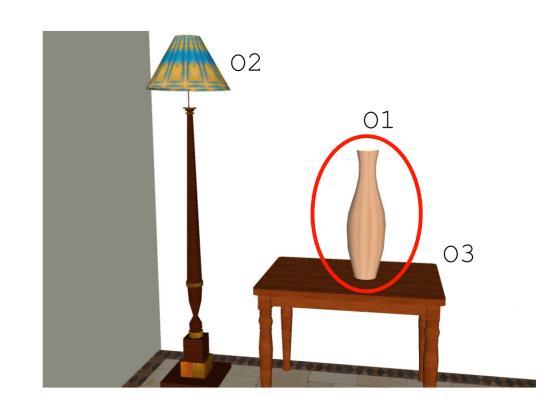
Goal: refer to 01

Strategy 1: speak the truth (Maxim of Quality)

on 03 right of 02

Problem: ambiguity

Strategy 2: also be unambiguous (Maxims of Quality and Manner)



Goal: refer to 01

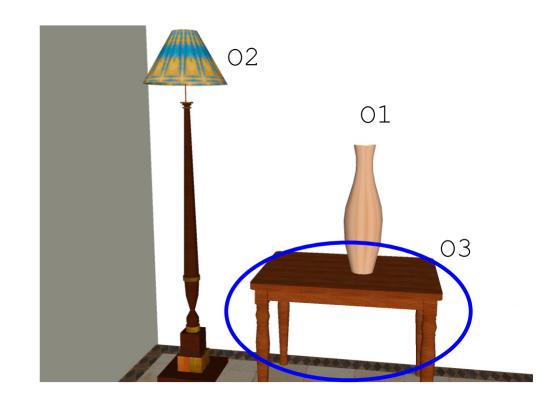
Strategy 1: speak the truth (Maxim of Quality)

on 03 right of 02

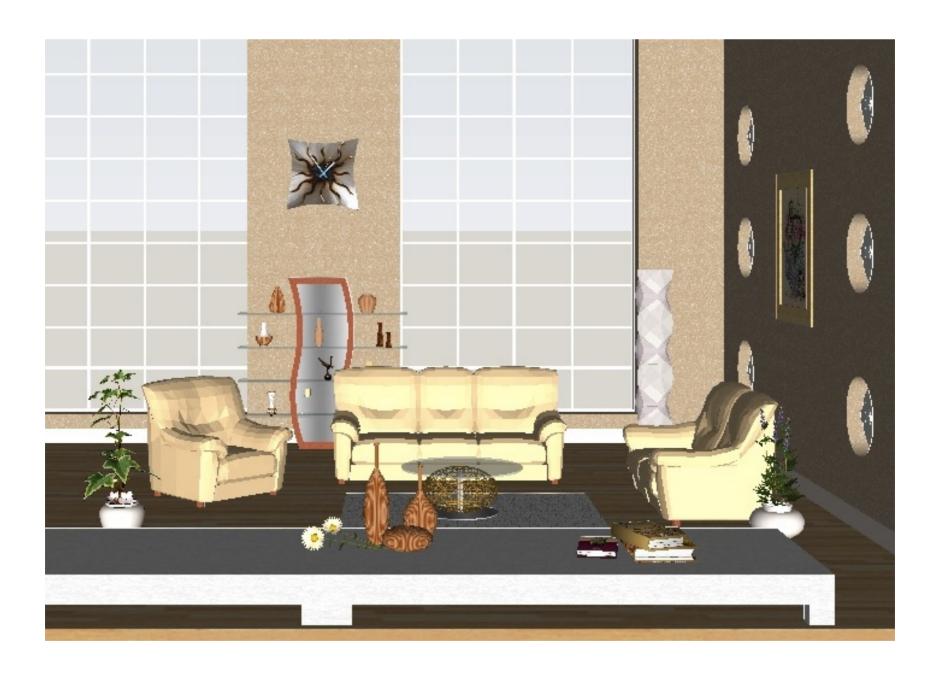
Problem: ambiguity

Strategy 2: also be unambiguous (Maxims of Quality and Manner)

on 03



# Actual Example



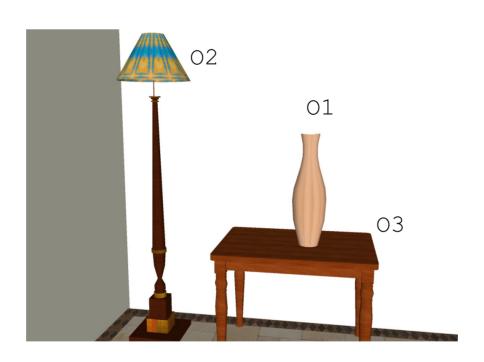
speaker

speaker

listener

speaker

listener

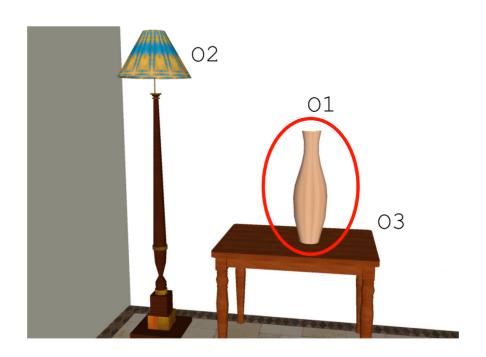


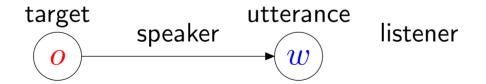
target

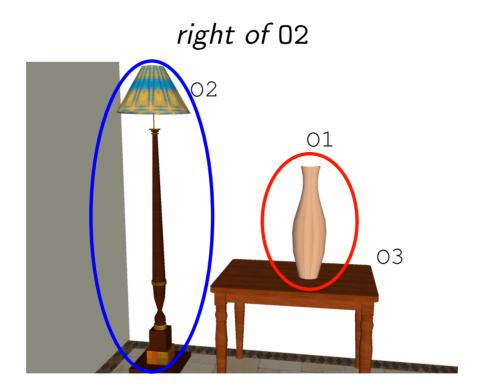


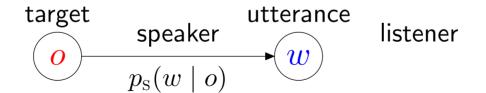
speaker

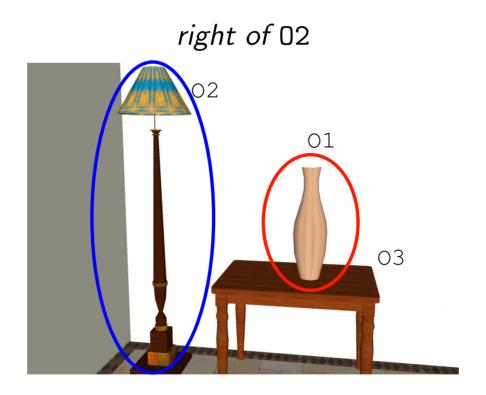
listener

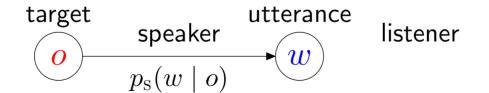


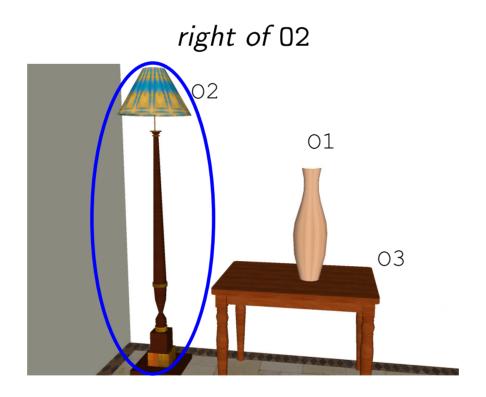


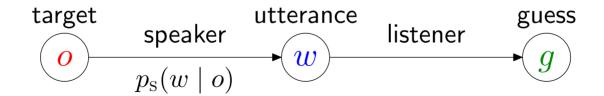


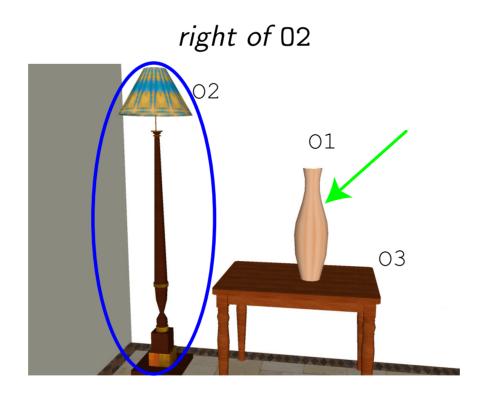


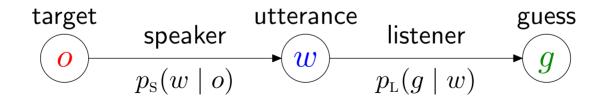


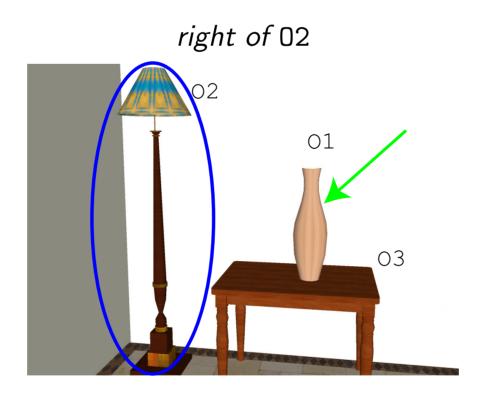


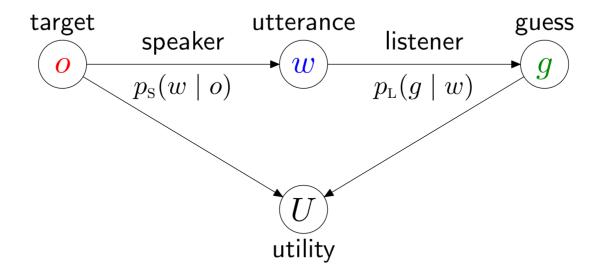




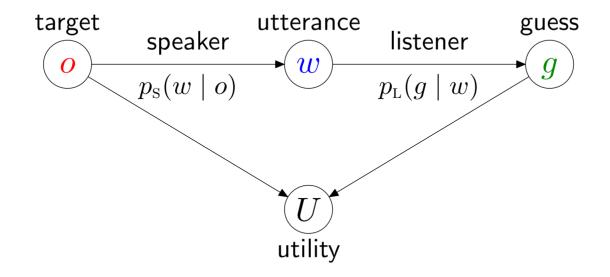








$$U(o,g) = \mathbb{I}[o=g] = \begin{cases} 1 & \text{if } o = g \\ 0 & \text{otherwise} \end{cases}$$



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$$\mathsf{EU}(\mathbf{S}, \mathbf{L}) = \mathbb{E}_{\mathbf{S}, \mathbf{L}}[U(o, g)]$$

## Speaker Strategies

Assign scores to utterances via:

$$p_{\scriptscriptstyle ext{S}}(w|o)$$

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Two speaker strategies:

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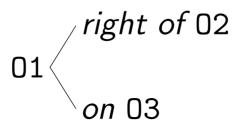
$$p_{\scriptscriptstyle ext{S}}(w|o)$$

Two speaker strategies:

- 1. semantics only (Maxim of Quality)
- 2. semantics + pragmatics + (Maxims of Quality + Manner)

## Semantics Only

Game tree:



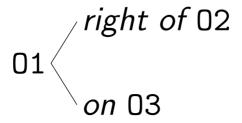
### Semantics Only

Game tree:

 $p_{\mathrm{S}}(w|o)$  depends only on truth of utterance, does not need to take listener into account

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Game tree:



 $p_{\mathrm{S}}(w|o)$  depends only on truth of utterance, does not need to take listener into account

Reflex speaker because it does not consider consequence of actions.

Maximize wrt.  $p_{\rm S}(w|o)$ :

$$\mathsf{EU}(\mathrm{S},\mathrm{L}) = \mathbb{E}_{\mathrm{S},\mathrm{L}}[U(o,g)]$$

Maximize wrt.  $p_s(w|o)$ :

$$\mathsf{EU}(\mathrm{S}, \mathrm{L}) = \mathbb{E}_{\mathrm{S}, \mathrm{L}}[U(o, g)]$$

 $p_{\rm S}(w|o)$  determinstically says:

$$\operatorname{argmax}_{w'} p_{\scriptscriptstyle 
m L}(o \mid w')$$

Maximize wrt.  $p_s(w|o)$ :

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Needs embedded model of listener:  $p_{\rm L}(o|w)$ 

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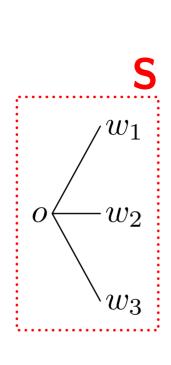
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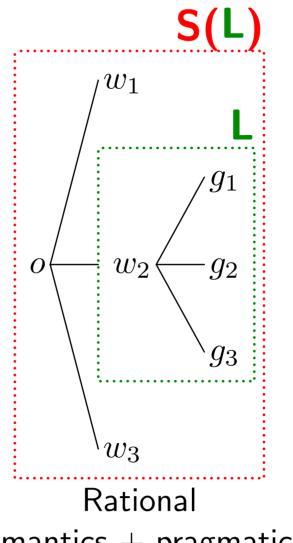
Needs embedded model of listener:  $p_{\rm L}(o|w)$ 

Rational speaker because it is optimal with respect to given listener.

#### Reflex vs. Rational

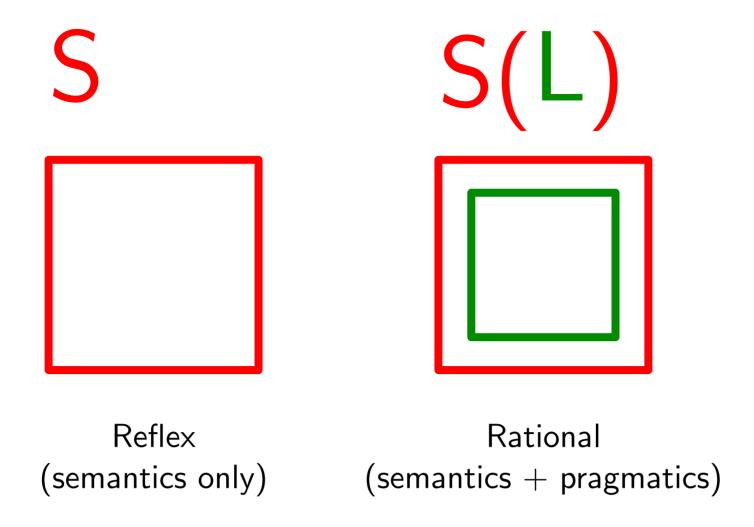


Reflex (semantics only)



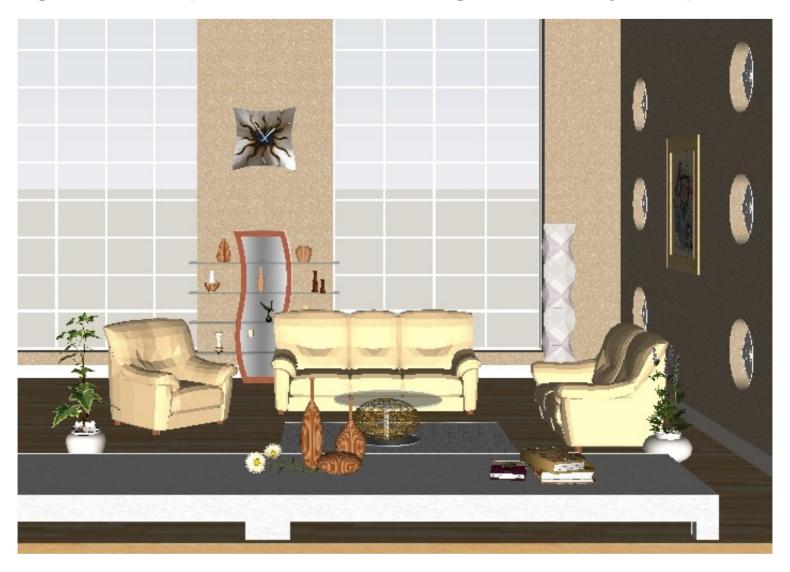
(semantics + pragmatics)

#### Reflex vs. Rational

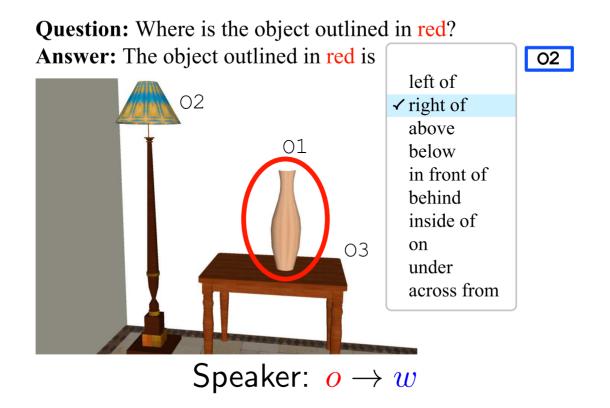


## **Experimental Setup**

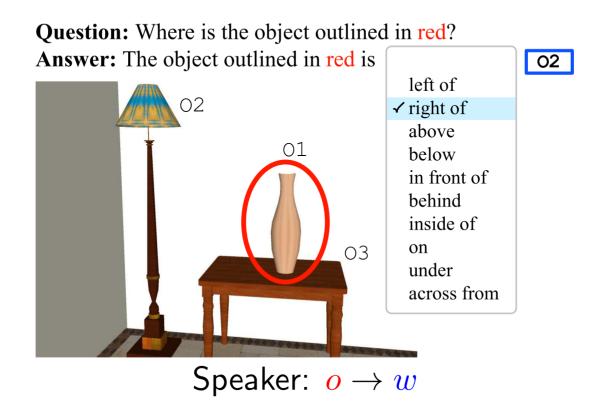
Google sketchup: 43 rooms, average of 22 objects per room



#### Data Collection with Mechanical Turk



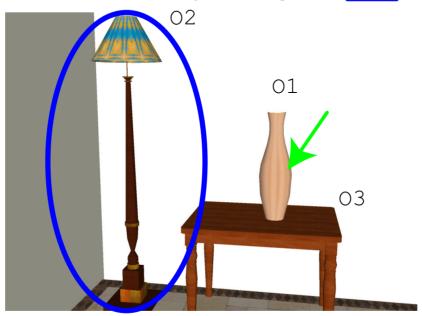
### Data Collection with Mechanical Turk



Yields annotated data:

$$\{(o_1,w_1),\cdots,(o_n,w_n)\}$$

**Question:** What object is **right of** 2?



Listener:  $w \rightarrow g$ 

Given  $p_{\rm S}(\boldsymbol{w}|\boldsymbol{o})$ , and  $(\boldsymbol{o_1},\ldots,\boldsymbol{o_n})$ ,

```
Given p_{\mathrm{S}}(\pmb{w}|\pmb{o}), and (\pmb{o_1},\ldots,\pmb{o_n}), s generates: (\pmb{w_1},\ldots,\pmb{w_n})
```

```
Given p_{\mathrm{S}}(w|o), and (o_1,\ldots,o_n), so generates: (w_1,\ldots,w_n) where: w_i = \mathrm{argmax}_w \ p_{\mathrm{S}}(w|o_i)
```

Given  $p_{s}(\boldsymbol{w}|\boldsymbol{o})$ , and  $(\boldsymbol{o_1},\ldots,\boldsymbol{o_n})$ ,

S generates:

$$(w_1,\ldots,w_n)$$

where:

$$\mathbf{w_i} = \operatorname{argmax}_{\mathbf{w}} p_{\mathrm{S}}(\mathbf{w}|\mathbf{o_i})$$

turkers generate:

$$(g_1,\ldots,g_n)$$

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turkers generate:

$$(g_1,\ldots,g_n)$$

compute success metric:

Success(s) = 
$$\frac{1}{n} \sum_{i} \mathbb{I}[\mathbf{o_i} = g_i]$$

Given  $p_{\rm S}(w|o)$ , and  $(o_1,\ldots,o_n)$ ,

S generates:

$$(w_1,\ldots,w_n)$$

where:

$$\mathbf{w_i} = \operatorname{argmax}_{\mathbf{w}} p_{\mathrm{S}}(\mathbf{w}|\mathbf{o_i})$$

turkers generate:

$$(g_1,\ldots,g_n)$$

compute success metric:

Success(s) = 
$$\frac{1}{n} \sum_{i} \mathbb{I}[\mathbf{o_i} = g_i]$$

Note: only collecting data and evaluating are done by humans.

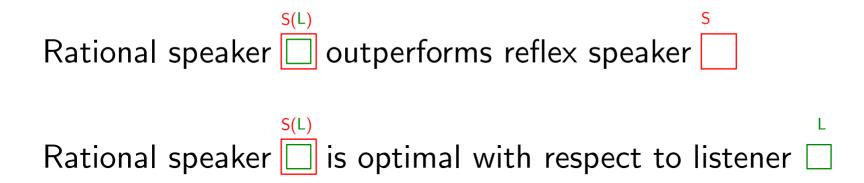
## Results

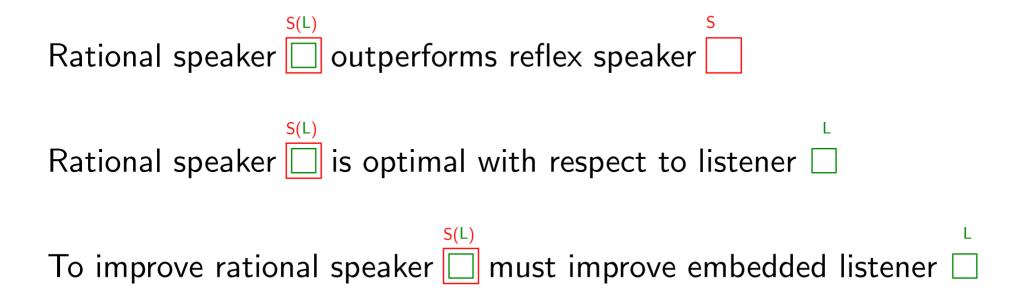
LITERAL agents put mass uniformly on true outputs

Speaker	Success
Reflex LITERAL	4.6%
Rational LITERAL	33.7%

Rational speaker outperforms reflex speaker.

Rational speaker outperforms reflex speaker





Rational speaker outperforms reflex speaker Rational speaker is optimal with respect to listener.

To improve rational speaker must improve embedded listener.

Up next: extensions for improving the listener model.

### Listener Extensions

- Training a Listener
- Generating Complex Utterances
- Modeling Listener Confusion

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Before: listener was LITERAL

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Now: learn from mturk data:

$$\{(o_1, w_1), \ldots, (o_n, w_n)\}$$

Before: listener was LITERAL

Now: learn from mturk data:

$$\{(o_1, w_1), \ldots, (o_n, w_n)\}$$

Train a log-linear model:

$$p_{\text{LEARNED}}(g|w; \theta_{\text{L}}) \propto \exp\{\theta_{\text{L}}^{\top}\phi(g, w)\}$$

Before: listener was LITERAL

Now: learn from mturk data:

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Use it to define the rational LEARNED speaker

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Train a log-linear model:

$$p_{\text{LEARNED}}(g|w; \theta_{\text{L}}) \propto \exp\{\theta_{\text{L}}^{\top}\phi(g, w)\}$$

Use it to define the rational LEARNED speaker

We also train  $p_{\rm S}(w|o;\theta_{\rm S})$  using the same data and features to get the reflex Learned speaker

The features  $\phi(g,w)$  are defined between:

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 $\bullet$  guess object g



The features  $\phi(g, w)$  are defined between:

- $\bullet$  guess object g
- w = right of 02



The features  $\phi(g, w)$  are defined between:

ullet guess object g

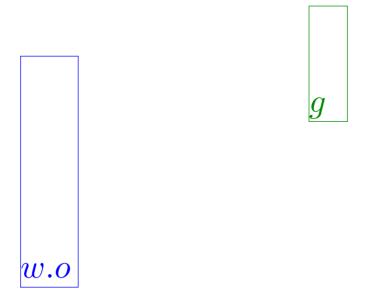
• 
$$w = \underbrace{right \ of}_{w.r} \underbrace{02}_{w.o}$$



Features inspired by [Regier, 2001; Tellex, 2009; Landau, 1993]

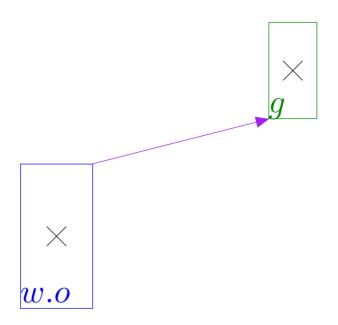
The features  $\phi(g, w)$  are defined between:

- ullet guess object g
- $w = \underbrace{right \ of \ 02}_{w.o}$
- $\bullet$  g and w.o are bounding boxes

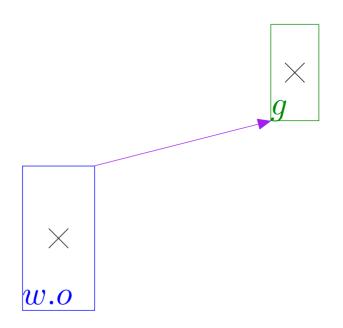


Features inspired by [Regier, 2001; Tellex, 2009; Landau, 1993]

# Distance Features

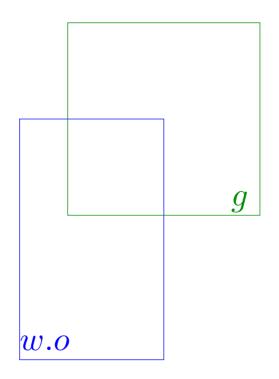


### Distance Features

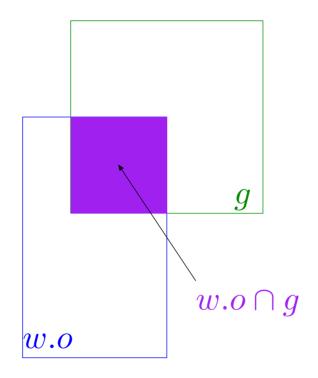


```
\phi_{dist} = value of shortest distance between g and w.o
\phi_{top1} = \mathbb{I}[g \text{ is closest to } w.o]
\phi_{top5} = \mathbb{I}[g \text{ is among top 5 closest to } w.o]
\phi_{top10} = \mathbb{I}[g \text{ is among top 10 closest to } w.o]
```

# Containment Features



## Containment Features

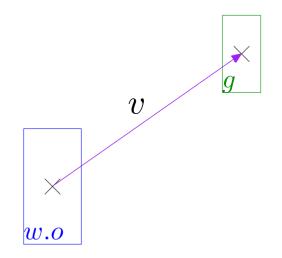


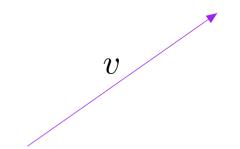
$$\phi_{cont2} = \operatorname{vol}(\underline{w.o} \cap \underline{g}) / \operatorname{vol}(\underline{g})$$

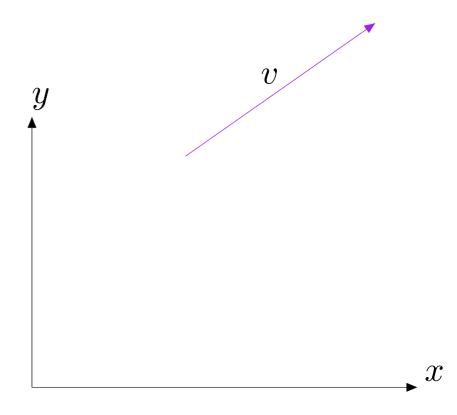
$$\phi_{cont1} = \mathsf{vol}(\underline{w.o} \cap \underline{g}) \ / \ \mathsf{vol}(\underline{w.o})$$

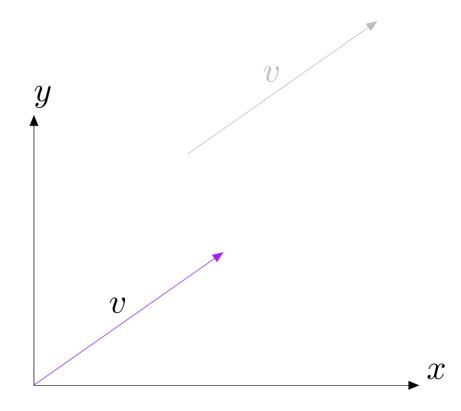


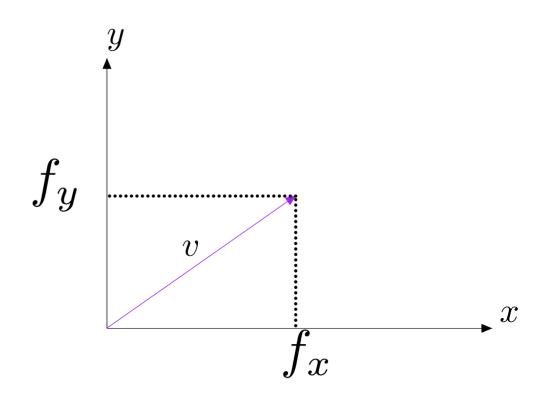












$$\phi_{projx} = f_x$$

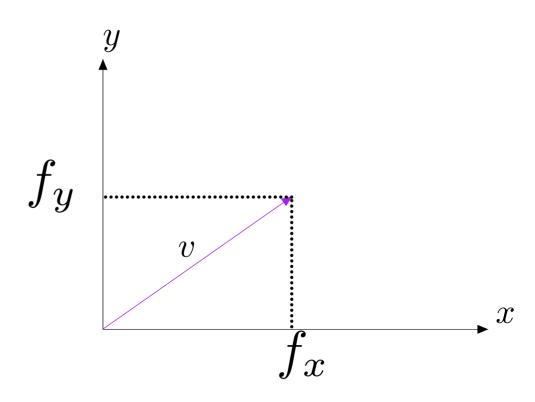
$$\phi_{projy} = f_y$$

$$\phi_{projz} = f_z$$

$$\phi_{proj1} = \mathbb{I}[f_x = \max\{f_x, f_y, f_z\}]$$

$$\phi_{proj2} = \mathbb{I}[f_y = \max\{f_x, f_y, f_z\}]$$

$$\phi_{proj3} = \mathbb{I}[f_z = \max\{f_x, f_y, f_z\}]$$



Speaker	Success
S	
Reflex LITERAL	4.6%
S(L)	
Rational LITERAL	33.7%

<u>Speaker</u>	Success
Reflex LITERAL	4.6%
Rational LITERAL	33.7%
Reflex LEARNED	38.4%
Rational LEARNED	52.6%

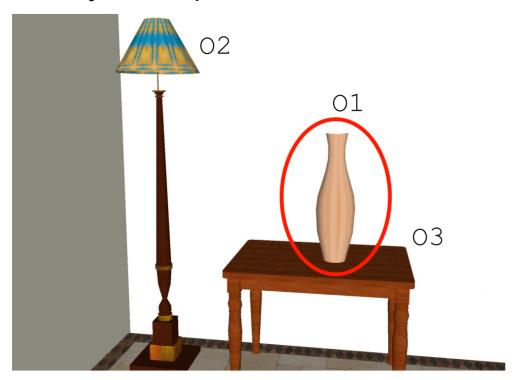
Two things are missing from the setup so far.

Two things are missing from the setup so far.

1. Arbitrary descriptors

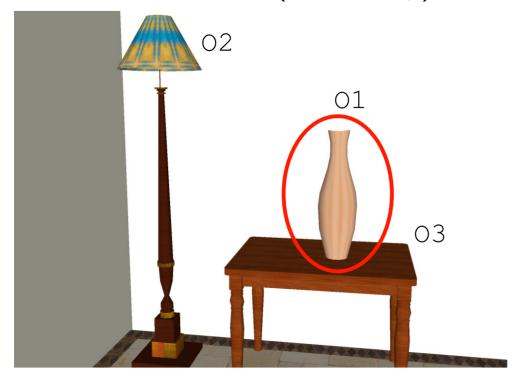
Two things are missing from the setup so far.

#### 1. Arbitrary descriptors



Two things are missing from the setup so far.

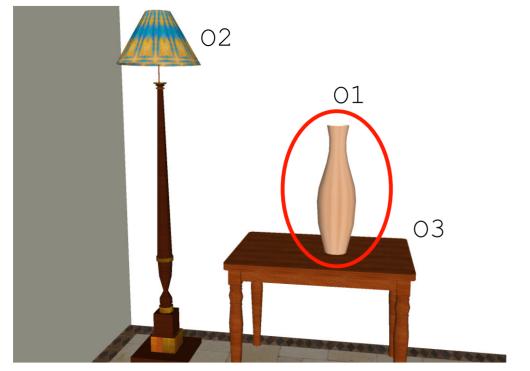
1. Arbitrary descriptors (not today)



2

Two things are missing from the setup so far.

1. Arbitrary descriptors (not today)

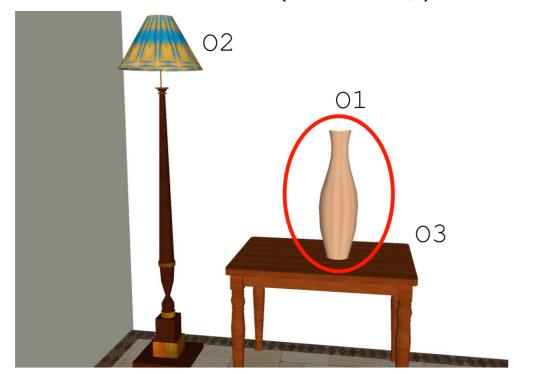


We will not be seeing 100% in this talk.

2.

Two things are missing from the setup so far.

1. Arbitrary descriptors (not today)

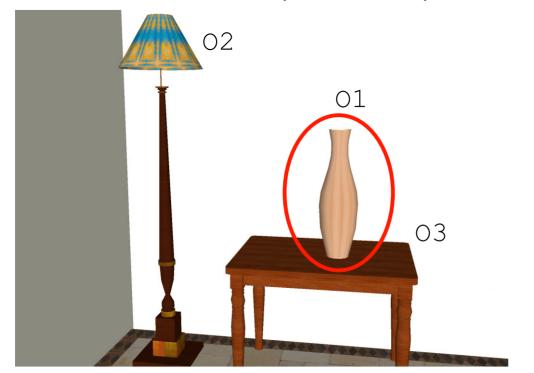


We will not be seeing 100% in this talk.

#### 2. Complex utterances

Two things are missing from the setup so far.

1. Arbitrary descriptors (not today)



We will not be seeing 100% in this talk.

2. Complex utterances (coming up)

#### Listener Extensions

- Training a Listener
- Generating Complex Utterances
- Modeling Listener Confusion

Before: utterances were simple, such as:

right of 02

on 03

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Now: utterances are from grammar:

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right of 02

on 03

Now: utterances are from grammar:

[noun]

 $ext{N} 
ightarrow something} \mid ext{O1} \mid ext{O2} \mid \cdots$ 

Before: utterances were simple, such as:

right of 02

on 03

Now: utterances are from grammar:

[noun]  $N \rightarrow something \mid 01 \mid 02 \mid \cdots$  [relation]  $R \rightarrow on \mid right \ of \mid \cdots$ 

Before: utterances were simple, such as:

right of 02

on 03

Now: utterances are from grammar:

```
[noun] N \rightarrow something | 01 | 02 | \cdots
```

[relation]  $R \rightarrow on \mid right \ of \mid \cdots$ 

[relativization] RP  $\rightarrow$  R NP

Before: utterances were simple, such as:

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Now: utterances are from grammar:

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[noun] N \rightarrow something \mid 01 \mid 02 \mid \cdots
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[relativization] RP  $\rightarrow$  R NP

right of 02

Before: utterances were simple, such as:

right of 02

on 03

Now: utterances are from grammar:

```
 \begin{array}{lll} \text{[noun]} & \text{N} \rightarrow \textit{something} \mid \texttt{O1} \mid \texttt{O2} \mid \cdots \\ & \text{R} \rightarrow \textit{on} \mid \textit{right of} \mid \cdots \\ & \text{[relativization]} & \text{RP} \rightarrow \text{RNP} \end{array}
```

elativizationj nr 7 mm

on something right of 02

Before: utterances were simple, such as:

right of 02

on 03

Now: utterances are from grammar:

[noun]

 $N \rightarrow something \mid 01 \mid 02 \mid \cdots$ 

[relation]

 $R o on \mid right \ of \mid \cdots$ 

[relativization] RP  $\rightarrow$  R NP

[conjunction]

 $NP \rightarrow NRP^*$ 

Before: utterances were simple, such as:

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on 03

Now: utterances are from grammar:

```
[noun] N \rightarrow something \mid 01 \mid 02 \mid \cdots
```

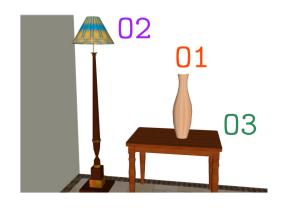
[relation]  $R \rightarrow on \mid right \ of \mid \cdots$ 

[relativization] RP  $\rightarrow$  R NP

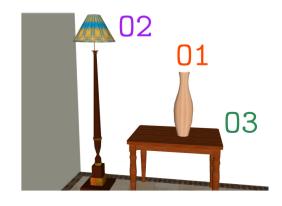
[conjunction]  $NP \rightarrow NRP^*$ 

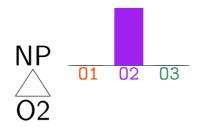
right of 02 and on 03

Computing:  $p(g \mid on something right of 02)$ 



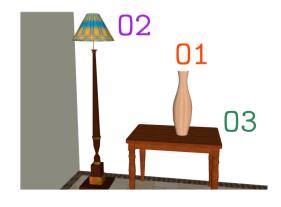
Computing:  $p(g \mid on something right of 02)$ 

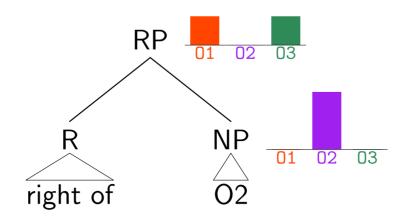




If w is rooted at N,  $p_{\scriptscriptstyle L}(g|w)=\mathbb{I}[w=g]$ .

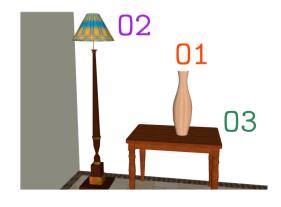
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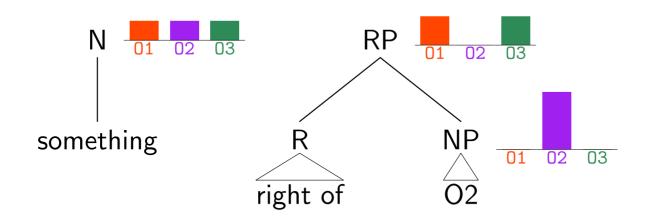




If w is rooted at RP, recurse on NP subtree, use base listener.

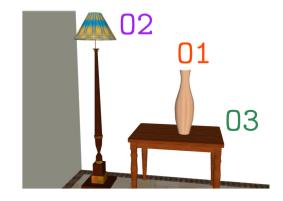
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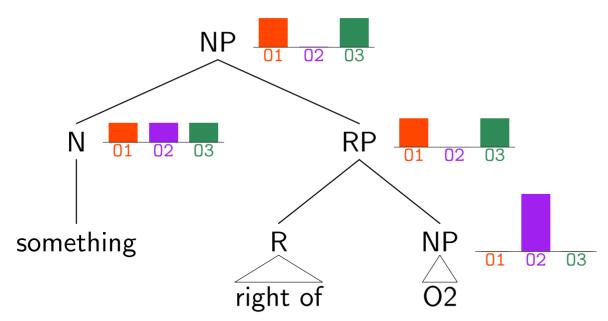




If w is rooted at N and w = something,  $p_{\rm L}(g|w)$  is uniform.

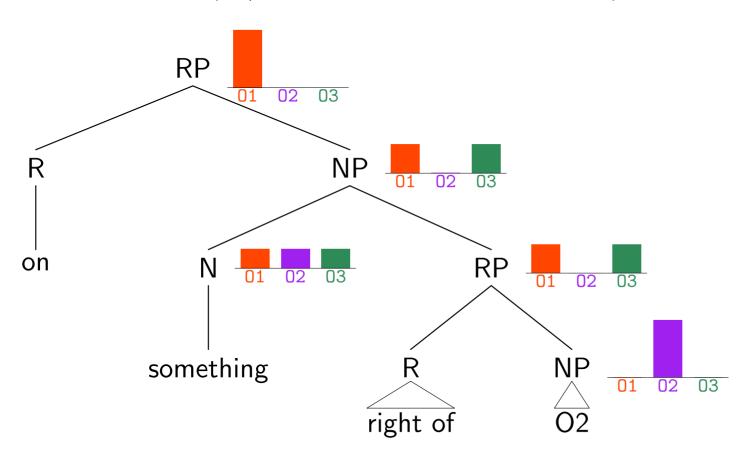
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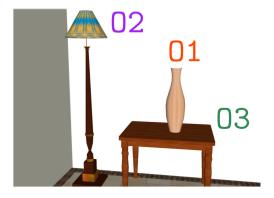




If w is rooted at NP, recurse on children, multiply and renormalize.

Computing:  $p(g \mid on something right of 02)$ 





If w is rooted at RP, recurse on NP subtree, use base listener.

Speaker	Success
Reflex LEARNED	38.4%
Rational LEARNED	52.6%

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Problem: introducing complex utterances hurts success

Observations: success is lower

Observations: success is lower & all uterances are longer

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Is longer always better?

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Is longer always better?

Right of the lamp

Observations: success is lower & all uterances are longer

Is longer always better?

Right of the lamp and on the table

Observations: success is lower & all uterances are longer

Is longer always better?

Right of the lamp and on the table and below the ceiling

Observations: success is lower & all uterances are longer

Is longer always better?

Right of the lamp and on the table and below the ceiling and in the room

Observations: success is lower & all uterances are longer

Is longer always better?

Right of the lamp and on the table and below the ceiling and in the room and etc.

### Listener Confusion

Observations: success is lower & all uterances are longer

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Right of the lamp and on the table and below the ceiling and in the room and etc.

Maxim of manner: also be brief

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• saves time

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Observations: success is lower & all uterances are longer

Is longer always better?

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Maxim of manner: also be brief

- saves time
- prevents confusion

### Listener Extensions

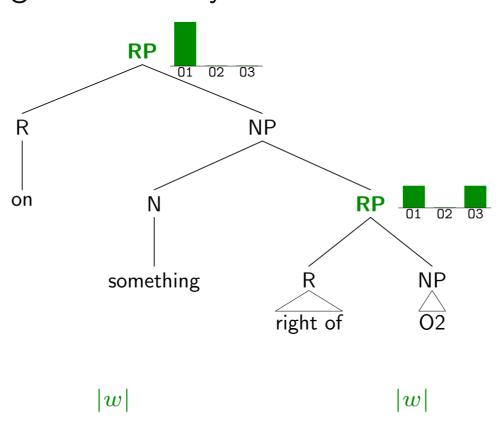
- Training a Listener
- Generating Complex Utterances
- Modeling Listener Confusion

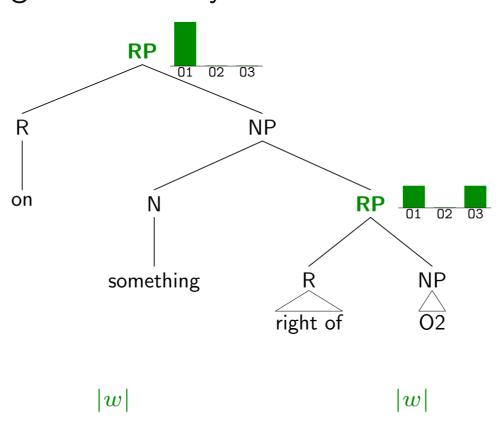
Problem: our model does not match turkers

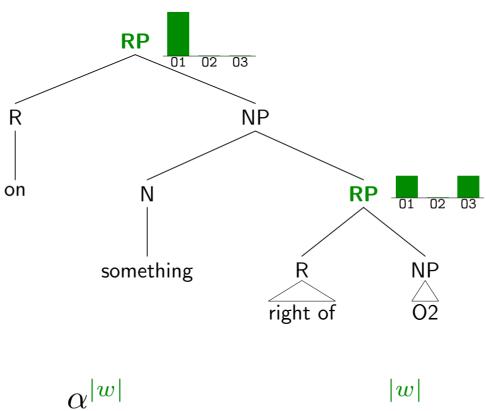
|w|

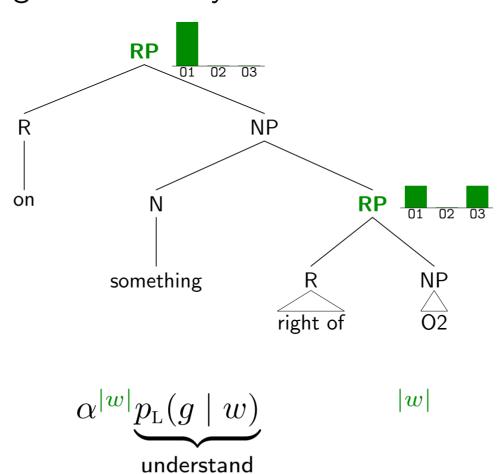
Problem: our model does not match turkers Confused turkers guess randomly.

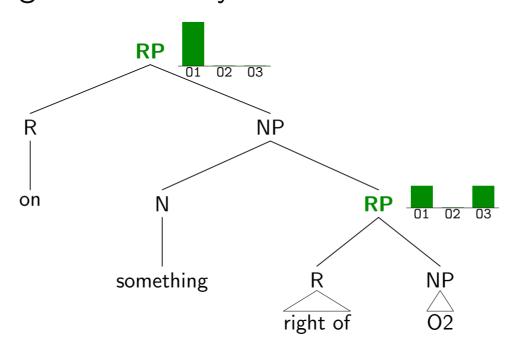
|w| |w|



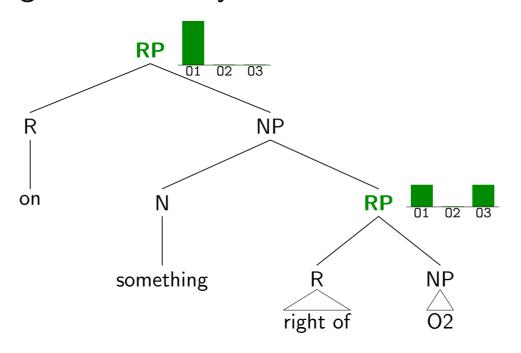




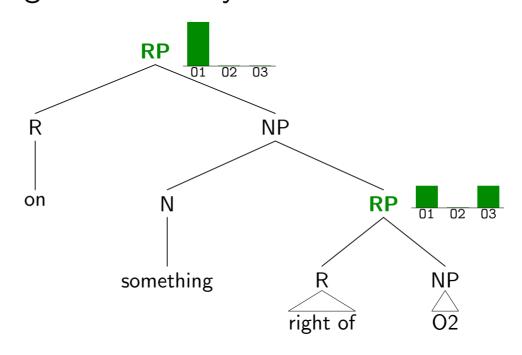




$$\alpha^{|w|} \underbrace{p_{\mathrm{L}}(g \mid w)}_{\text{understand}} + (1 - \alpha^{|w|})$$



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$$\tilde{p}_{\mathrm{L}}(g \mid w) = \alpha^{|w|} \underbrace{p_{\mathrm{L}}(g \mid w)}_{\text{understand}} + (1 - \alpha^{|w|}) \underbrace{p_{\mathrm{rnd}}(g \mid w)}_{\text{confused}}$$

## Results

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Rational LEARNED	compositional	51.0%

# Results

<u>Speaker</u>	Success
Rational LEARNED	52.6%
Rational LEARNED compositional	51.0%
Rational LEARNED +confusion mod	del 54.5%

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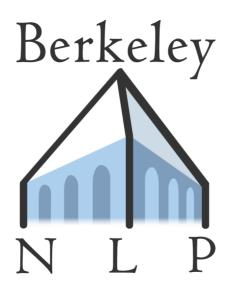
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#### Meanwhile:

Landau (1993), Regier (2001), and Tellex (2009) have been studying spatial language

Our contribution: we show how a game theoretic pragmatics model can be used to successfully generate spatial descriptions

# Thank you!



slides compiled with rfig